

# Pinned Frames

- Multiforce Members
- End Reactions
- Member Forces
- Stability
- Lateral Bracing

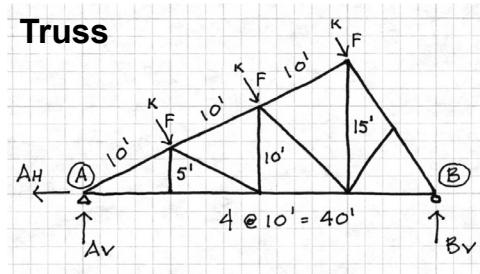


Das Spitzhäuschen. Marktplatz. Bernkastel-Kues

## Pinned Frame vs. Truss

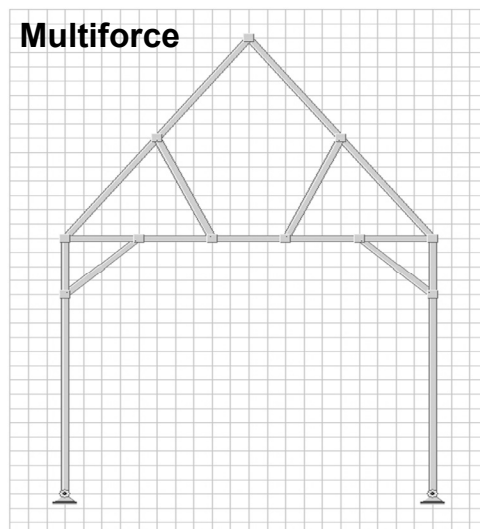
Trusses:

- 2-force members
- rigid bodies

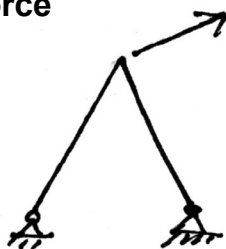


Pinned Frames:

- 2-force or multiforce (axial or bending)
- rigid body or mechanism

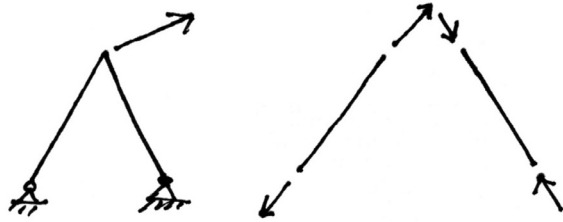


**2-force**

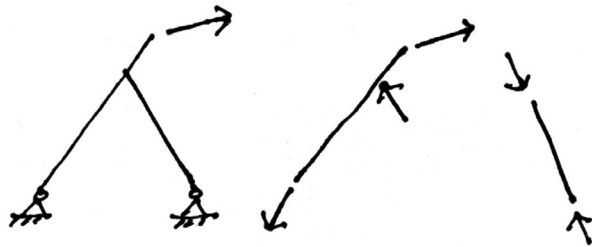


# Frame Types

Frames with 2-force members  
(axial forces)



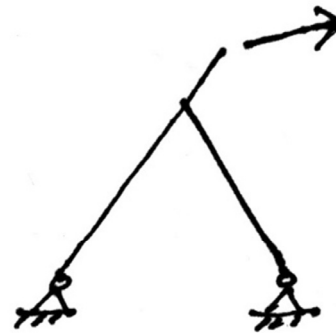
Frames with multiforce members  
(bending + axial forces)



# Rigidity

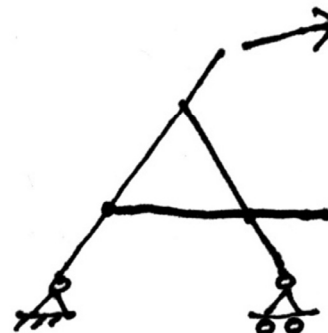
**Nonrigid frames** (require 4 or more  
reaction components for stability)

Without supports they collapse.



**Rigid frames** (only require 3 reaction  
components)

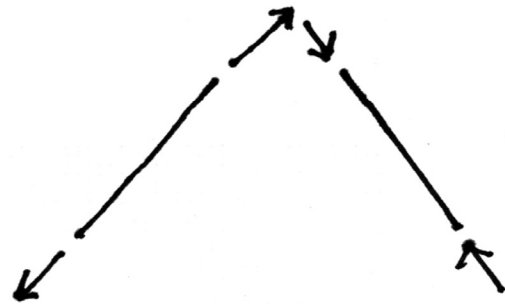
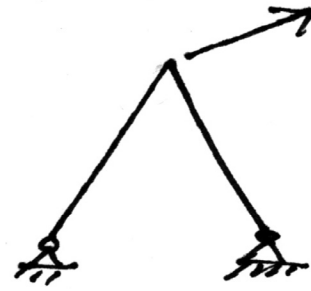
Remain a rigid body even without  
supports.



## 2-Force Member Frames

### Procedure

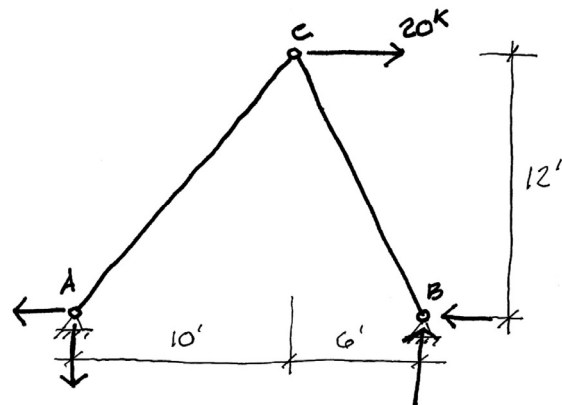
1. Solve external supports
  - FBDs
  - Simultaneous equations
2. Cut FBD of each member
3. Solve member forces



## 2-Force Member Frames

### Analysis

1. Solve external supports
  - FBDs
  - Simultaneous equations



$$\sum M @ A = 0 = 20(12) - B_v(16)$$
$$B_v = 15^k$$

$$\sum F_v = 0 = -A_v + B_v$$
$$A_v = 15$$

# 2-Force Member Frames

## Analysis

2. Cut FBD of each member

For 2-force members the force components follow the slope.

BY SLOPE

$$\frac{6}{5} : \frac{15}{12.5}$$

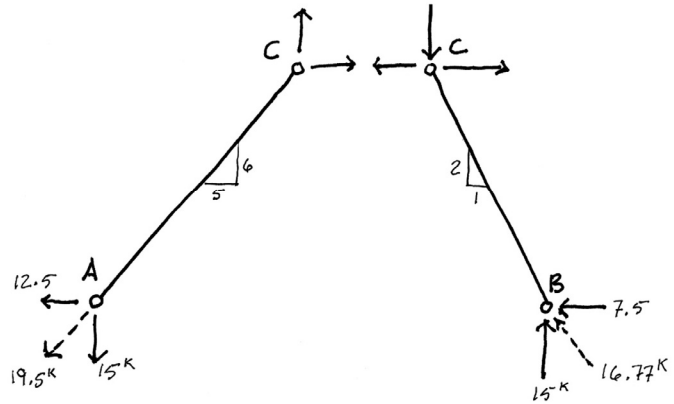
BY SLOPE

$$\frac{2}{1} : \frac{15}{7.5}$$

REACTION COMPONENTS

$$B_V = 15\text{K} \uparrow$$

$$B_H = 7.5 \leftarrow$$



# 2-Force Member Frames

## Analysis

3. Check member forces and balance forces.

LEFT FBD

$$\sum F_V = 0 = -15 + C_V$$

$$C_V = 15\text{K}$$

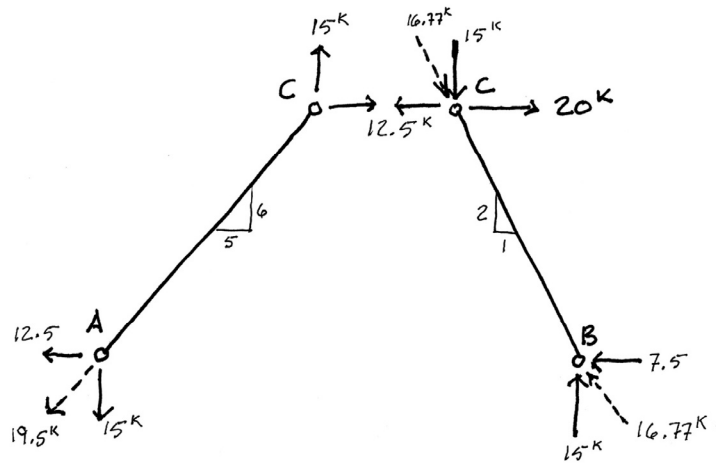
RIGHT FBD

$$\sum F_V = 0 = 15\text{K} - C_V$$

$$C_V = 15\text{K}$$

$$\sum F_H = 0 = 20\text{K} - 7.5 - C_H$$

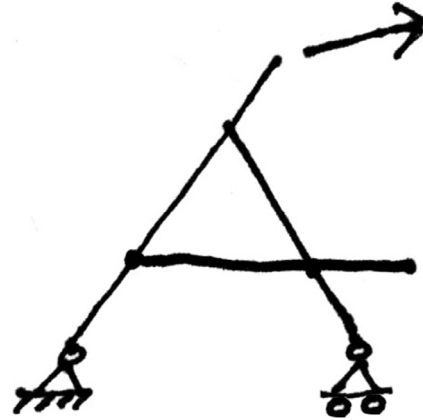
$$C_H = 12.5\text{K}$$



# Multiforce Member Frames

## Procedure

1. Solve external supports
2. Cut FBD of each member
3. Solve forces at joints.
4. Some members will be multiforce, they will be in bending.



## Analysis

1. Solve external supports

Get vertical components by summing moments.

$$\sum M_{@A} = 0$$

$$20^k(12') + 15^k(20') - B_v(20') = 0$$

$$B_v = \underline{27^k \uparrow}$$

$$\sum F_v = 0$$

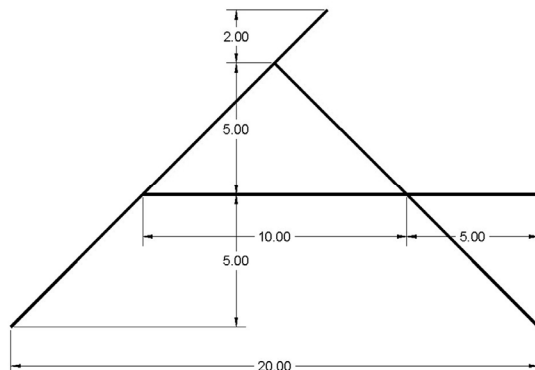
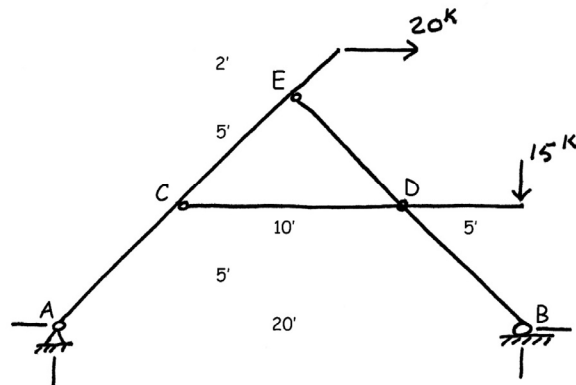
$$-A_v - 15^k + 27^k = 0$$

$$A_v = \underline{12^k \downarrow}$$

$$\sum F_H = 0$$

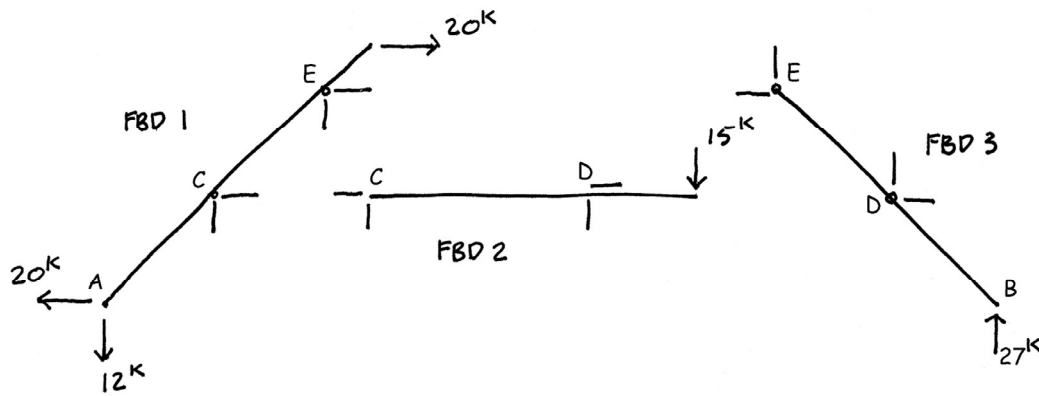
$$-A_H + 20^k = 0$$

$$A_H = \underline{20^k \leftarrow}$$



# Analysis

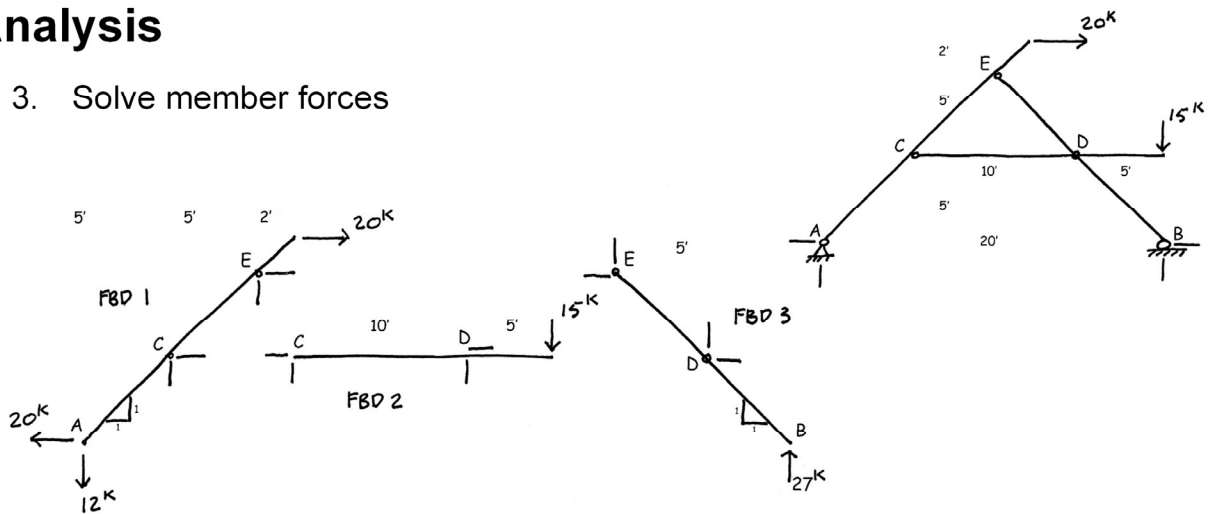
## 2. Cut FBD of each member



- Work between the FBDs using 3 equations of statics.
- End force components can be solved as axial and normal forces.
- The normal forces are “shear” forces and result in moments or “bending” forces.
- Not all systems are statically determinate and may then require other methods.

# Analysis

## 3. Solve member forces



FBD 2

$$\sum M_e D = 0 = -C_v(10') + 15\text{ k}(5')$$

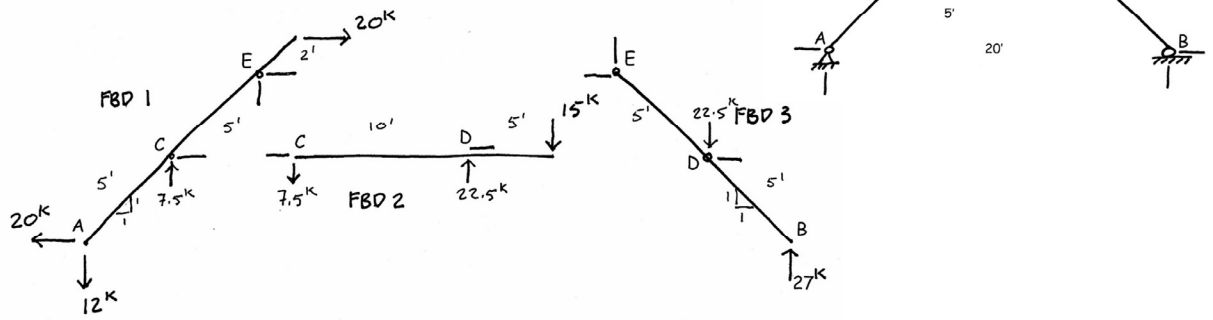
$$C_v = 7.5\text{ k}$$

$$\sum F_v = 0 = -7.5\text{ k} + D_v - 15\text{ k}$$

$$D_v = 22.5\text{ k}$$

# Analysis

3. Solve member forces



FBD 1

$$\sum M_E = 20^k(10') - 12^k(10') + 7.5^k(5') - C_H(5') + 20^k(2') = 0$$

$$200 - 120 + 37.5 - C_H(5) + 40 = 0$$

$$C_H = 31.5^k$$

$$\sum F_V = 0 = -12^k + 7.5^k + E_V$$

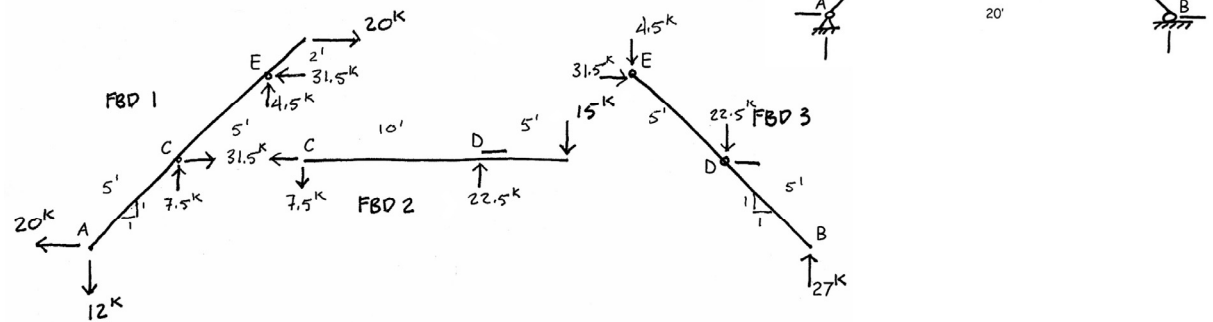
$$E_V = 4.5^k$$

$$\sum F_H = 0 = -20^k + 31.5^k - E_H + 20^k$$

$$E_H = 31.5^k$$

# Analysis

3. Solve member forces



FBD 2

$$\sum F_H = 0 = -31.5^k + D_H$$

$$D_H = 31.5^k$$

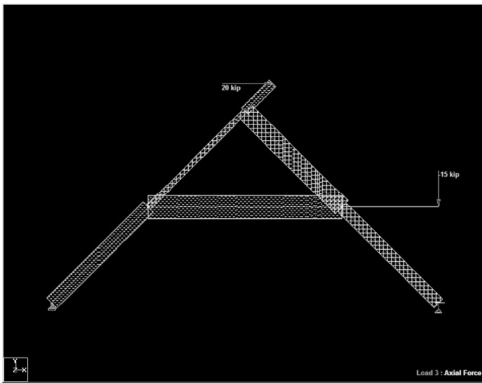
FBD 3 - CHECK

$$\sum F_H = 31.5^k - 31.5^k = 0 \quad \checkmark$$

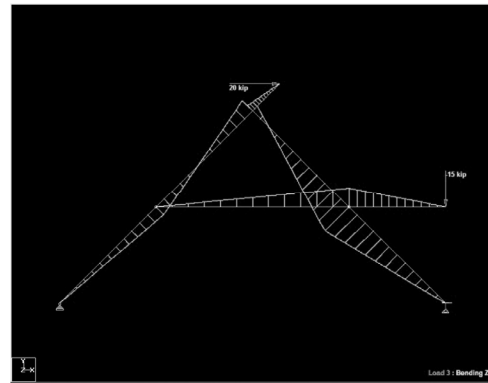
$$\sum F_V = -4.5^k - 22.5^k + 27^k = 0 \quad \checkmark$$

# Analysis

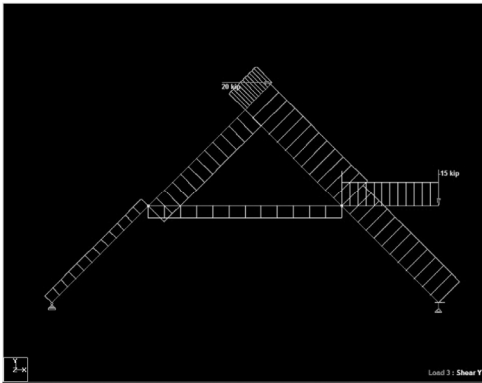
## 4. Determine multforce members



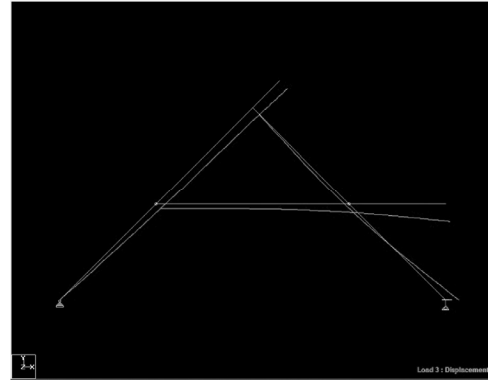
Axial Force



Bending Moment



Shear Force



Deflection

## Riverbend Timber Framing

<https://www.riverbendtf.com/>



Marty Birkenkamp





# Pariseau Barn

## Example



# Pariseau Barn Example



Motise and Tenon Joint



## Pariseau Barn Example



## Pariseau Barn Example



# Pariseau Barn Example

