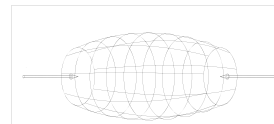


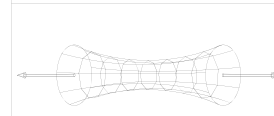
# Stress and Strain

- Stress
- Strain
- Analysis – ASD vs. LRFD
- Modes of Failure

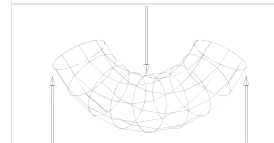
$$\sigma = \frac{P}{A}$$



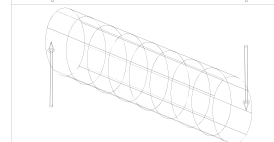
$$\sigma = \frac{P}{A}$$



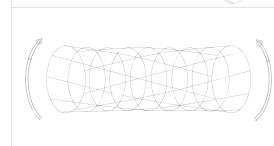
$$\sigma = \frac{M c}{I}$$



$$\tau = \frac{P}{A} \text{ or } \frac{VQ}{Ib}$$



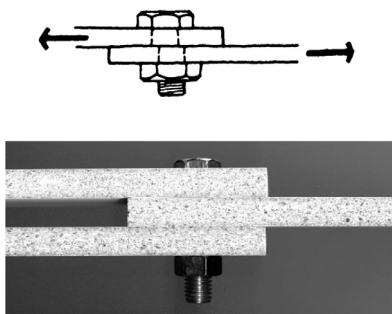
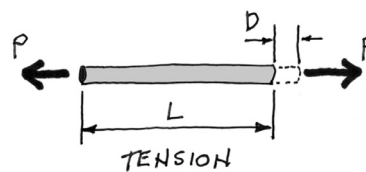
$$\tau = \frac{T r}{J}$$



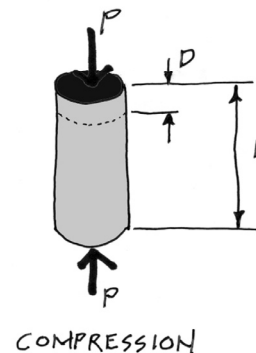
## Stress

Stress is the result of some force being applied to an area of some material.

$$\sigma = \frac{P}{A}$$



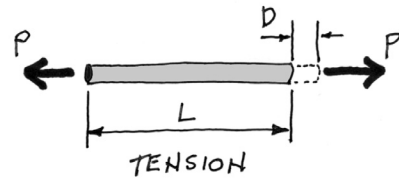
Shear Stress



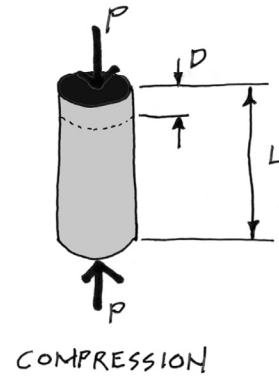
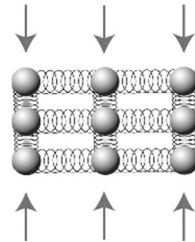
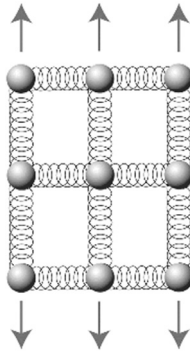
# Strain

Strain is the amount of deformation in the material, per unit length.

$$\epsilon = \frac{D}{L}$$



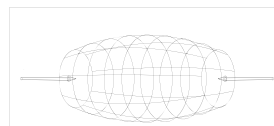
Deformation occurs either in stretching (tension) or in compressing (compression) but not always at the same rate.



# Types of Stress

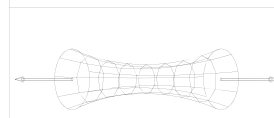
- Compression

$$\sigma = \frac{P}{A}$$



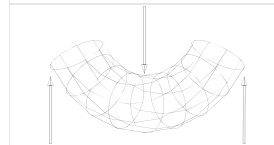
- Tension

$$\sigma = \frac{P}{A}$$



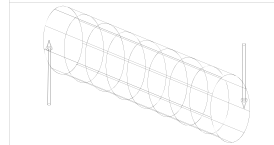
- Flexure

$$\sigma = \frac{M c}{I}$$



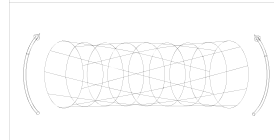
- Shear

$$\tau = \frac{P}{A} \text{ or } \frac{VQ}{Ib}$$



- Torsion

$$\tau = \frac{T r}{J}$$



# Stress Analysis

## Allowable Stress Design (ASD)

- use design loads (no F.S. on loads)
- reduce stress by a Factor of Safety F.S.

$$f_{actual} = \frac{P}{A}$$

$$f_{actual} \leq F_{allowable}$$

$$F_{allowable} = F.S. \cdot f_{yield}$$

## Load & Resistance Factored Design (LRFD)

- Use loads with safety factor  $\gamma$
- Use factor on ultimate strength  $\phi$

$$P_{load} = \gamma \cdot P_{applied}$$

$$P_{load} \leq P_{resisting}$$

$$P_{resisting} = \phi \cdot P_{material}$$

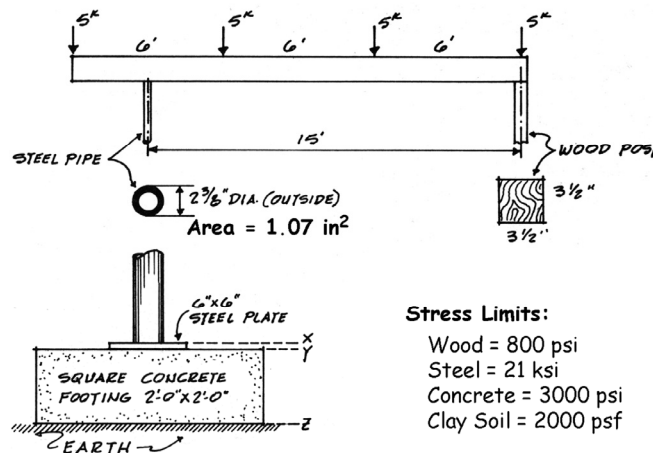
# Stress Calculations

Find the stress in each material

## Axial Compression

The stress equals the force spread over an area.

$$\sigma = \frac{P}{A}$$

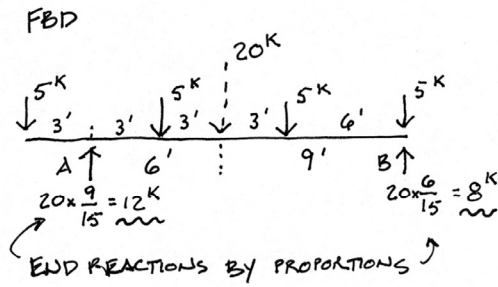
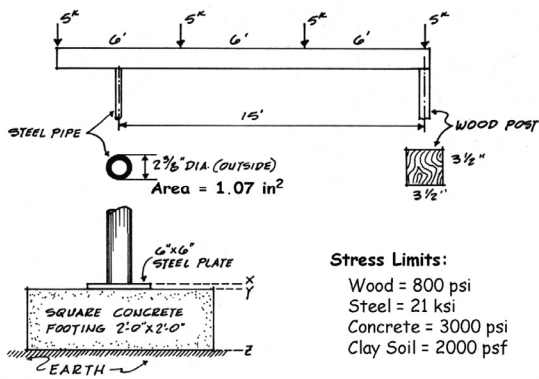


### Stress Limits:

Wood = 800 psi  
 Steel = 21 ksi  
 Concrete = 3000 psi  
 Clay Soil = 2000 psf

# Stress Calculations

FBD – reactions



OR

$\Sigma M$  AT EACH REACTION

$$\Sigma M @ A = -5k(3') + 5k(3') + 5k(9') + 5k(15') - B(15')$$

$$B = 8k$$

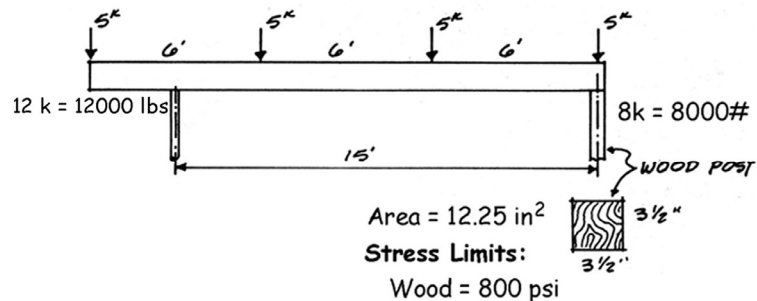
$$\Sigma F_v = 0 = -20 + A + B = 0$$

$$A = 12k$$

# Stress Calculations

The stress equals the force spread over an area.

$$\sigma = \frac{P}{A}$$



Stress in Wood:

$$f = P/A$$

$$f = 8000\text{lbs}/12.25\text{in}^2$$

$$f = 653\text{psi}$$

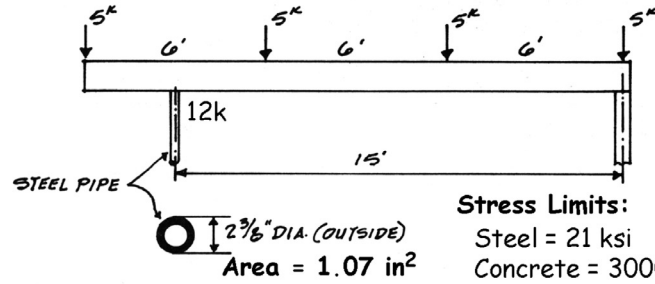
$$F = 800\text{psi}$$

$$f < F \text{ ok}$$

# Stress Calculations

The stress equals the force spread over an area.

$$\sigma = \frac{P}{A}$$

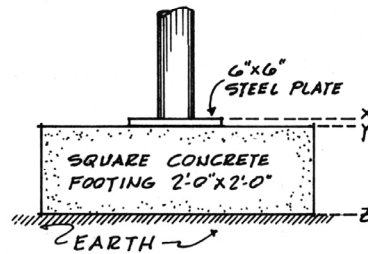


**Stress Limits:**  
 Steel = 21 ksi  
 Concrete = 3000 psi

**Stress in Steel:**  
 $f = P/A = 12k / 1.07 \text{ in}^2$   
 $f = 11.2 \text{ ksi} < F = 21 \text{ ksi}$  ok

**Stress in Concrete:**  
 $f = 12000 \text{ lbs} / 1.07 \text{ in}^2$   
 $f = 11200 \text{ psi} > 3000 \text{ psi}$  FAILS!

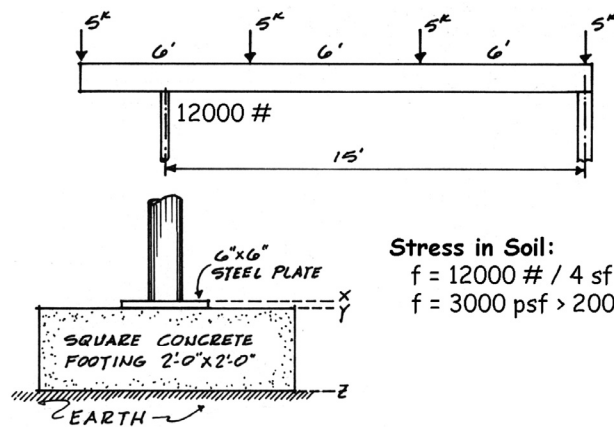
$f = 12000 / 36 = 333 \text{ psi}$   
 $333 \text{ psi} < 3000 \text{ psi}$  ok



# Stress Calculations

The stress equals the force spread over an area.

$$\sigma = \frac{P}{A}$$



**Stress in Soil:**  
 $f = 12000 \# / 4 \text{ sf}$   
 $f = 3000 \text{ psf} > 2000 \text{ psf}$  FAILS!

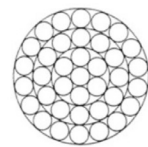
**Stress Limits:**  
 Clay Soil = 2000 psf

# Stress Calculations

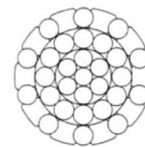
## Axial Tension

The stress equals the force spread over an area.

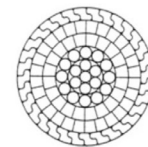
$$\sigma = \frac{P}{A}$$



open spiral rope



half-locked rope



full-locked rope



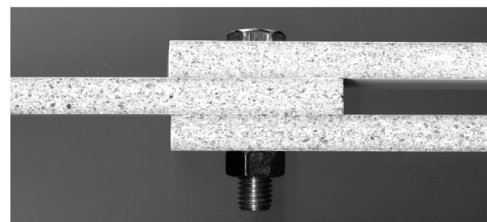
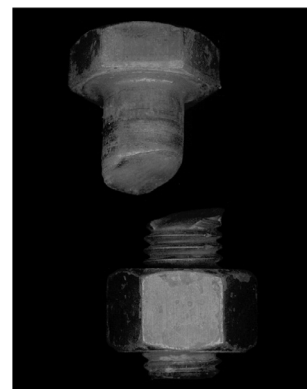
Santiago Calatrava - Serreria Bridge - Valencia 2008

# Stress Calculations

## Shear

The stress equals the force spread over an area.

$$\sigma = \frac{P}{A}$$



# Stress Calculations

## Bending

### Flexure Stress

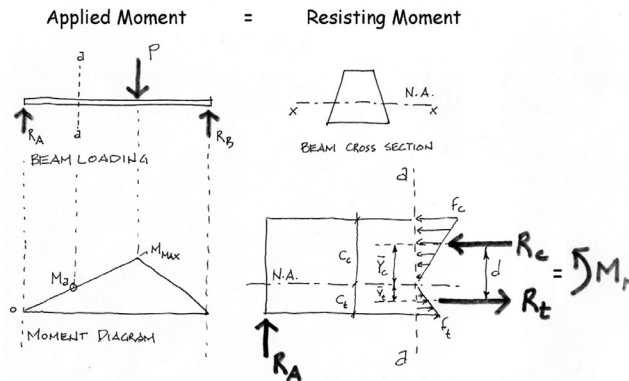
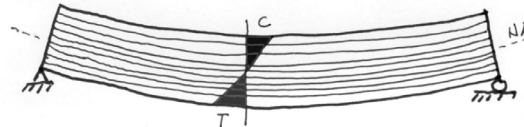
The stress is on the “fibers” or longitudinal layers

$$\sigma = \frac{M c}{I}$$

### Shear Stress

The stress is between the longitudinal layers.

$$\tau = \frac{VQ}{Ib}$$



# Modes of Failure

## Strength

- Tension rupture
- Compression crushing

## Stability

- Column buckling
- Beam lateral torsional buckling

## Serviceability

- Beam deflection
- Building story drift
- cracking

