

3. Shear and Moment by Semi-graphical Method – diagram relationships

By recognizing the diagrammatic relationships between curves and their derivatives and integrals, shear and moment diagrams can be constructed based on areas and slopes of those curves.

Moving from Upper to Lower Diagrams:

- The area between any two points on the upper diagram is equal to the change in value between same points on the lower diagram.
- The degree of the curve increases by one for each diagram.
- The value on the upper diagram is equal to the slope of the lower diagram.
- Where the upper diagram crosses 0 on the axis, the lower diagram is at a maximum or minimum.
- Points of inflection or "contraflexure" (between + and – curvature) on the elastic curve (deflected shape) are points of zero moment.



3. Semi-graphical Method



3. Semi-graphical Method

Procedure:

- 1. Find end reactions
- 2. Start at left end of V-Diagram and "apply" load from left to right
- 3. Calculate areas of V-Diagram
- Find max. and min. values on M-Diagram using V-Diagram areas between axis crossings.
- 5. Check slope and + or values



3. Semi-graphical Method

example

Cantilever Beam



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Structures I

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3. Semi-graphical Method

example

Beam with cantilever



3. Semi-graphical Method

example





4. Superposition of Equations

Equations of shear or moment may be combined (superimposed) for any number of cases.

BUT

The appropriate location along the beam for which the equation is valid must be maintained

Thus

At the reaction, V = P/2 + wL/2

And at the C.L. $M = PL/4 + wL^2/8$





4. Superposition of Equations - example

find x at M_{max} for combined asymmetric cases





Moment Diagram vs. Catenary Curve

For a gravity loaded simple span beams, the shape of the of the moment diagram is the inverse of the catenary curve.

