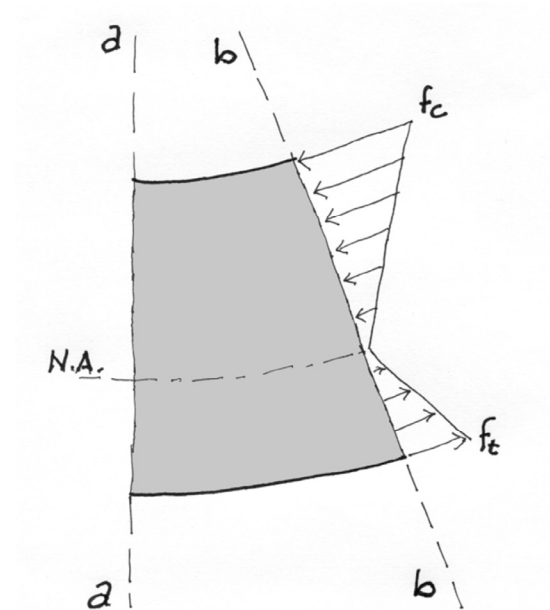


# Bending Stresses in Beams

- Elastic Bending
- Stress Equation
- Section Modulus
- Flexure Capacity Analysis
- Flexure Beam Design

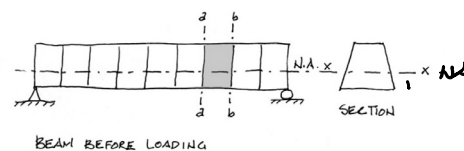


## Elastic Bending

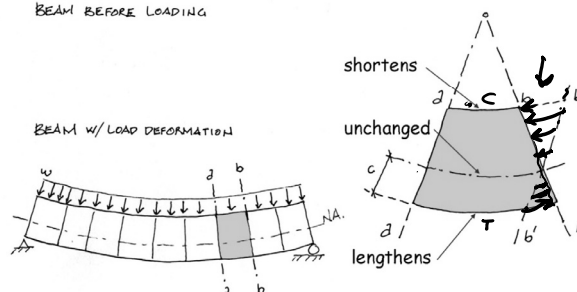
Flexure results in internal tension and compression forces, the resultants of which form a couple which resists the applied moment.



In the initial unloaded state, all transverse sections are parallel.



The application of load causes the member to bend in a curve. This means the initial parallel plane sections, while remaining plane, now follow the radii of the curves.

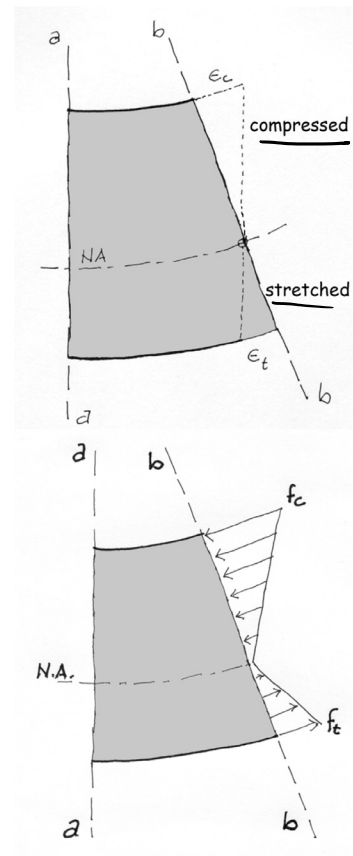


Notice that by the geometry of the curved member the top edge is shortened and the bottom edge is lengthened. Only the neutral axis remains its original length.

# Elastic Bending

The change in lengths, top and bottom, results in the material straining. For a simple span with downward loading, the top is compressed and the bottom stretched. The change in length is linear and proportional to the distance from the Neutral Axis.

The material strains result in corresponding stresses. By **Hooke's Law**, these stresses are proportional to the strains which are proportional to the change in length of the radial arcs of the beam "fibers". This assumes that the Modulus of Elasticity is constant across the section.



# Elastic Bending

The applied moment at any point on the beam is equal to the resisting moment which is formed by the internal force couple,  $R_c$  and  $R_t$ .

$$\boxed{M_{\text{applied}} = M_{\text{resisting}}} \quad \text{Applied Moment} = \text{Resisting Moment}$$

*STRENGTH OF MATERIAL*

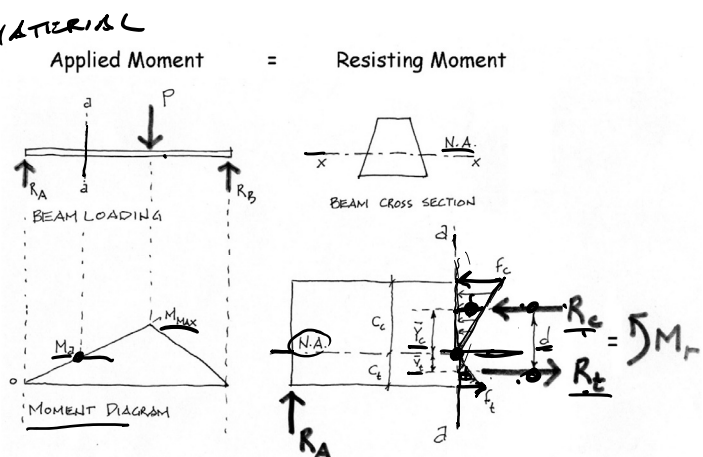
Balance of the external and internal moments

$$\boxed{R_{\text{comp.}} = R_{\text{tens.}}}$$

Balance of the internal force couple

$$\boxed{\begin{aligned} M_r &= R_c \cdot y_c + R_t \cdot y_t \\ M_r &= R_c \cdot d \checkmark \\ M_r &= R_t \cdot d \checkmark \end{aligned}}$$

Expressions of the internal resisting moment



# Elastic Bending

The internal moment,  $M_r$ , can be expressed as the result of the couple  $R_c$  and  $R_t$

$$M_r = R_c \cdot \bar{y}_1 + R_t \cdot \bar{y}_2$$

In turn, the forces  $R_c$  and  $R_t$  can be written as the resultants of the "stress volumes" acting through the centroids of those volumes. The average unit stress,  $s = fc/2$  and so the resultant  $R$  is the area times  $s$ :

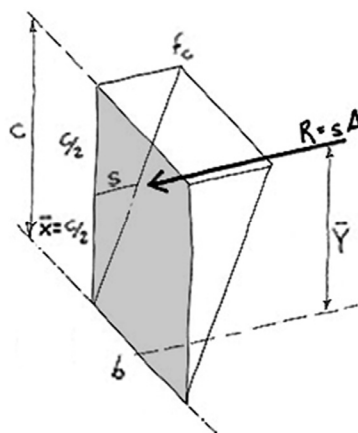
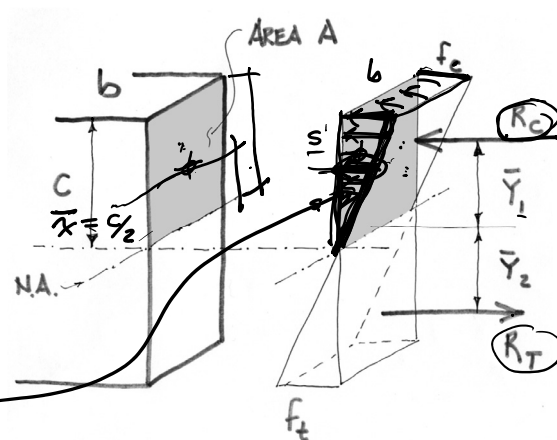
$$R = A \cdot s \quad \text{--- VOLUME}$$

Using similar triangles,  $s$  can be expressed as:

$$\frac{s}{f_c} = \frac{\bar{x}}{c} \quad \text{and} \quad s = \frac{f_c \cdot \bar{x}}{c}$$

Substituting these values back into the moment equation gives:

$$M_r = \frac{f_c A_c \bar{x}_1 \bar{y}_1}{c_c} + \frac{f_t A_t \bar{x}_2 \bar{y}_2}{c_t} = I$$



# Elastic Bending

By definition:

$$I_x = A \bar{x} \bar{y}$$

And for homogeneous materials with  $E_c = E_t$

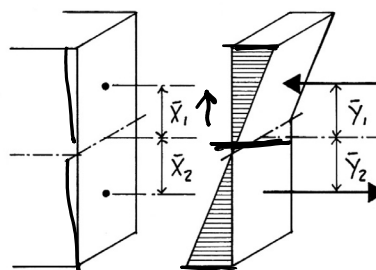
$$M_r = \frac{f I_1}{c} + \frac{f I_2}{c} = \frac{f}{c} (I_1 + I_2) \quad \text{--- TOTAL } I_x$$

Or using the  $I$  for the whole section:

$$M_r = \frac{f I_x}{c}$$

And so,

$$f = \frac{M c}{I} \quad \text{--- max } d/2$$



The Section Modulus is:

$$S = \frac{I}{c_{max}} = \frac{\frac{bd^3}{12}}{d/2} = \frac{bd^2}{6}$$

So, at extreme fibers:

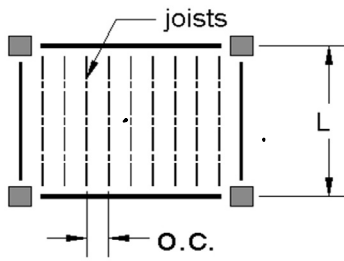
$$M = f S$$

And:

$$f = \frac{M}{S_x}$$

With  $c = h/2$  at extreme fibers of a symmetric section.

# Beam Analysis



Allowable Capacity (ASD):

$$M = F_b S$$

for steel:  $F_b = (0.66 \text{ to } 0.6) F_y$  ksi

for wood:  $F_b = 1000 \text{ to } 600$  psi

Applied Load:

$$M = \frac{wl^2}{8}$$

(uniform load)

Pass

$$\underbrace{M = F_b S}_{\text{STRENGTH}} > \underbrace{M = \frac{wl^2}{8}}_{\text{APPLIED LOAD}}$$

Fail

$$M = F_b S < M = \frac{wl^2}{8}$$

Capacity

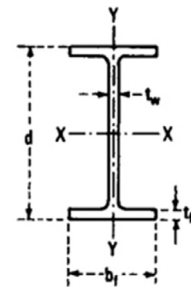
$$\underbrace{M = F_b S}_{\text{Capacity}} = \underbrace{M = \frac{wl^2}{8}}_{\text{Applied Load}} \text{ solve for } w$$

Design

$$\underbrace{M = \frac{wl^2}{8}}_{\text{Applied Load}} = \underbrace{M = F_b S}_{\text{Capacity}} \text{ solve for } S$$

## Beam Capacity Analysis - procedure

1. Determine section properties. (from table)
2. Choose safe allowable stress. (depends on bracing)
3. Calculate allowable moment capacity.  $M = F_b S$
4. Set equal to applied moment and find load.  $M = \frac{wl^2}{8}$



### WIDE FLANGE SHAPES

Section Number	Weight per Foot	Area of Section A	Depth of Section d	Flange		Web Thick-ness t <sub>w</sub>	Axis X-X			Axis Y-Y			r <sub>T</sub>
				Width b <sub>f</sub>	Thick-ness t <sub>f</sub>		I <sub>x</sub>	S <sub>x</sub>	r <sub>x</sub>	I <sub>y</sub>	S <sub>y</sub>	r <sub>y</sub>	
lb	in. <sup>2</sup>	in.	in.	in.	in.	in. <sup>4</sup>	in. <sup>3</sup>	in.	in. <sup>4</sup>	in. <sup>3</sup>	in.	in.	
W27 x	178	52.3	27.81	14.085	1.190	0.725	6990	502	11.6	555	78.8	3.26	3.72
	161	47.4	27.59	14.020	1.080	0.660	6280	455	11.5	497	70.9	3.24	3.70
	146	42.9	27.38	13.965	0.975	0.605	5630	411	11.4	443	63.5	3.21	3.68
W27 x	114	33.5	27.29	10.070	0.930	0.570	4090	299	11.0	159	31.5	2.18	2.58
	102	30.0	27.09	10.015	0.830	0.515	3620	267	11.0	139	27.8	2.15	2.56
	94	27.7	26.92	9.990	0.745	0.490	3270	243	10.9	124	24.8	2.12	2.53
	84	24.8	26.71	9.960	0.640	0.460	2850	213	10.7	106	21.2	2.07	2.49

# Beam Capacity Analysis - example

Given:

Beam = W27x178

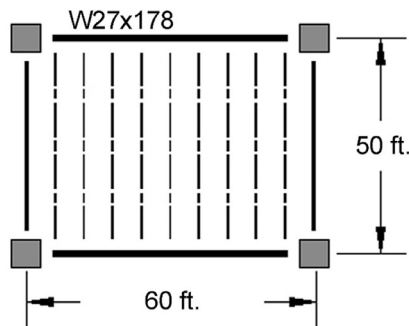
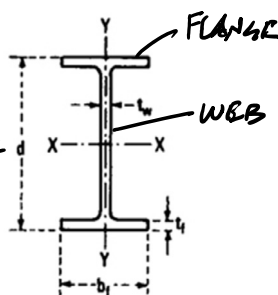
$S_x = 502 \text{ in}^3$

$F_y = 50 \text{ ksi}$

$F_b = .66F_y = 33 \text{ ksi}$  (braced by joists)

Find:

Floor capacity



## WIDE FLANGE SHAPES

Section Number	Weight per Foot	Area of Section A	Depth of Section d	Flange		Web Thickness $t_w$	Axis X-X			Axis Y-Y			$r_T$
				Width	Thickness		$I_x$	$S_x$	$r_x$	$I_y$	$S_y$	$r_y$	
				$b_f$	$t_f$		$\text{in}^4$	$\text{in}^3$	$\text{in.}$	$\text{in}^4$	$\text{in}^3$	$\text{in.}$	
<b>W27 x 178</b>	178	52.3	27.81	14.085	1.190	0.725	6990	502	11.6	555	78.8	3.26	3.72
161	161	47.4	27.59	14.020	1.080	0.660	6280	455	11.5	497	70.9	3.24	3.70
146	146	42.9	27.38	13.965	0.975	0.605	5630	411	11.4	443	63.5	3.21	3.68
<b>W27 x 114</b>	114	33.5	27.29	10.070	0.930	0.570	4090	299	11.0	159	31.5	2.18	2.58
102	102	30.0	27.09	10.015	0.830	0.515	3620	267	11.0	139	27.8	2.15	2.56
94	94	27.7	26.92	9.990	0.745	0.490	3270	243	10.9	124	24.8	2.12	2.53
84	84	24.8	26.71	9.960	0.640	0.460	2850	213	10.7	106	21.2	2.07	2.49

# Beam Capacity Analysis

Given:

Beam = W27x178

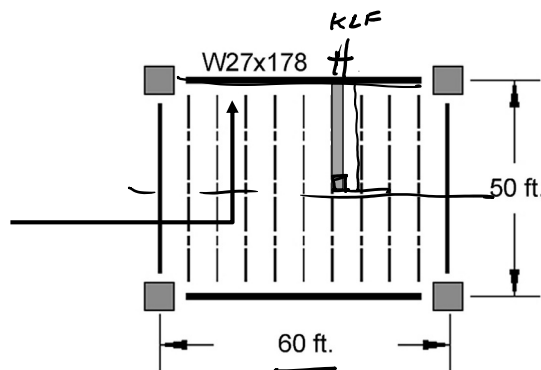
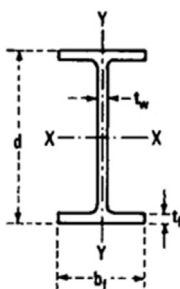
$S_x = 502 \text{ in}^3$

$F_y = 50 \text{ ksi}$

$F_b = .66F_y = 33 \text{ ksi}$  (fully braced)

Find:

Floor capacity



$$M = F_b S_x$$

$$M = \frac{33 \text{ ksi}}{502 \text{ in}^3} = 16566 \text{ K-in} = 1380.5 \text{ K-ft}$$

$$M = 1380.5 \text{ K-ft}$$

$$M = \frac{w l^2}{8} = 1380.5 \text{ K-ft}$$

$$w = \frac{M \cdot 8}{l^2} = \frac{1380.5 (8)}{60^2} = 3.068 \text{ K/ft} = 3068 \text{ #/ft}$$

$$\text{PSF} = \frac{w}{l/2} = \frac{3068}{50/2} = 123 \text{ PSF}$$

# Quiz

Given:

Beam = W27x14  
 $F_y = 36 \text{ ksi}$

$S_x = \text{in}^3$

$F_b = .6F_y = \text{ksi}$

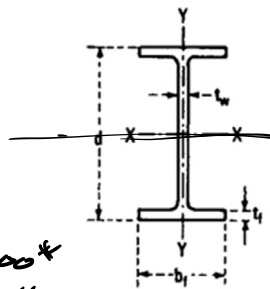
Find:

$$M_b = F_b S_x$$

Allowable Moment =

ft-lbs

$K = 1000^*$   
 $FT = 12''$



## WIDE FLANGE SHAPES

Section Number	Weight per Foot	Area of Section	Depth of Section	Flange			Axis X-X			Axis Y-Y			$r_T$
				Width	Thick-ness	Web Thick-ness	$I_x$	$S_x$	$r_x$	$I_y$	$S_y$	$r_y$	
	lb	in. <sup>2</sup>	in.	$b_f$	$t_f$	$t_w$	in. <sup>4</sup>	in. <sup>3</sup>	in.	in. <sup>4</sup>	in. <sup>3</sup>	in.	
W27 x 178	178	52.3	27.81	14.085	1.190	0.725	6990	502	11.6	555	78.8	3.26	3.72
161	161	47.4	27.59	14.020	1.080	0.660	6280	455	11.5	497	70.9	3.24	3.70
146	146	42.9	27.38	13.965	0.975	0.605	5630	411	11.4	443	63.5	3.21	3.68
→ W27 x 114	114	33.5	27.29	10.070	0.930	0.570	4090	299	11.0	159	31.5	2.18	2.58
102	102	30.0	27.09	10.015	0.830	0.515	3620	267	11.0	139	27.8	2.15	2.56
94	94	27.7	26.92	9.990	0.745	0.490	3270	243	10.9	124	24.8	2.12	2.53
84	84	24.8	26.71	9.960	0.640	0.460	2850	213	10.7	106	21.2	2.07	2.49

## Section Properties

### Section Modulus Table

Sorted by  $S_x$  for design selection

with:

$$S = I/c$$

$f_b$  is actual stress

$F_b$  is allowable stress

- for bracing  $< L_c$ ,  $F_b = 0.66F_y$
- for bracing  $< L_u$ ,  $F_b = 0.6F_y$

$F_y$  is the yield stress

$$M_r = .66F_y S_x$$

So the design equations is:

$$S_x = M_{\text{applied}} / F_b$$

Size

ALLOWABLE STRESS DESIGN SELECTION TABLE										
For shapes used as beams										
$F_y$	$L_c$	$L_u$	$M_R$	$S_x$	Shape	Depth $d$	$F_y$	$L_c$	$L_u$	$M_R$
Ksi	ft	ft	Kip-ft	in. <sup>3</sup>		in.	Ksi	ft	ft	Kip-ft
50							50			
10.6	11.2	2130	776	W 44x198	42%	—	12.5	15.5	1540	
14.1	15.2	2110	769	W 40x199	38%	—	16.6	20.0	1520	
11.8	45.7	2110	769	W 21x333	25	—	13.9	63.4	1520	
14.2	19.8	2080	757	W 33x221	33%	—	16.7	27.6	1500	
13.5	24.0	2050	746	W 30x235	31%	—	15.9	33.3	1480	
12.8	29.0	2040	742	W 27x258	29	—	15.1	40.3	1470	
10.9	15.1	1980	719	W 36x210	36%	—	12.9	20.9	1420	
11.9	34.7	1970	718	W 24x279	26%	—	14.0	48.2	1420	
12.8	16.7	1880	708	W 40x192	38%	37.1	17.8	19.7	1400	
11.6	42.7	1900	692	W 21x300	24%	—	13.7	59.4	1370	
14.1	17.9	1880	684	W 33x201	33%	—	16.6	24.9	1350	
10.6	12.3	1880	682	W 40x183	39	—	12.5	17.1	1350	
12.7	26.7	1850	674	W 27x235	28%	—	15.0	37.0	1330	
10.9	13.9	1830	664	W 36x194	36%	—	12.8	19.4	1310	
13.5	21.4	1820	663	W 30x211	31	—	15.9	29.7	1310	
11.8	31.4	1770	644	W 24x250	26%	—	13.9	43.7	1280	
11.5	39.2	1740	632	W 21x275	24%	—	13.6	54.5	1250	
12.6	24.9	1720	624	W 27x217	28%	—	14.9	34.5	1240	
10.8	49.0	1720	624	W 18x311	22%	—	12.7	68.1	1240	
10.8	13.1	1710	623	W 36x182	36%	—	12.7	18.2	1230	
10.4	11.0	1650	599	W 40x167	38%	—	12.5	14.5	1190	
13.5	19.4	1640	598	W 30x191	30%	—	15.9	26.9	1180	
11.7	29.0	1620	588	W 24x229	26	—	13.8	40.3	1160	
10.8	12.2	1600	569	W 36x170	36%	—	12.7	17.0	1150	
11.4	35.5	1560	569	W 21x248	23%	—	13.5	49.3	1130	
10.6	45.0	1550	564	W 18x283	21%	—	12.6	62.6	1120	
12.6	22.4	1530	556	W 27x194	28%	—	14.8	31.1	1100	
10.3	13.8	1510	549	W 33x169	33%	—	12.1	19.2	1090	
10.7	11.4	1490	542	W 36x160	36	—	12.7	15.7	1070	
13.4	17.5	1480	539	W 30x173	30%	—	15.8	24.2	1070	
11.7	26.5	1460	531	W 24x207	25%	—	13.7	36.7	1050	
10.5	42.2	1410	514	W 18x258	21%	—	12.4	58.6	1020	
8.5	10.7	1410	512	W 40x149	38%	—	11.9	12.8	1010	
11.4	32.7	1400	510	W 21x223	23%	—	13.4	45.4	1010	
10.5	11.3	1390	504	W 36x150	35%	—	12.6	14.6	998	
12.6	20.1	1380	502	W 27x178	27%	—	14.9	27.9	994	
11.6	24.7	1350	491	W 24x192	25%	—	13.7	34.3	972	
10.4	12.2	1340	487	W 33x152	33%	—	12.2	16.9	964	
10.4	38.8	1280	466	W 18x234	21	—	12.3	53.8	923	
11.3	29.8	1270	461	W 21x201	23	—	13.3	41.3	913	
12.6	18.3	1250	455	W 27x161	27%	—	14.8	25.4	901	
11.5	22.8	1240	450	W 24x176	25%	—	13.6	31.7	891	

# Beam Design - procedure

1. Choose a steel grade and allowable stress.

↗ ASSUME BRACING

2. Determine the applied moment (e.g. moment diagram)

3. Calculate the section modulus,  $S_x$

$$S_x = \frac{M}{F_b}$$

LOADS ↗  
↖

4. Choose a safe section. (from  $S_x$  table)

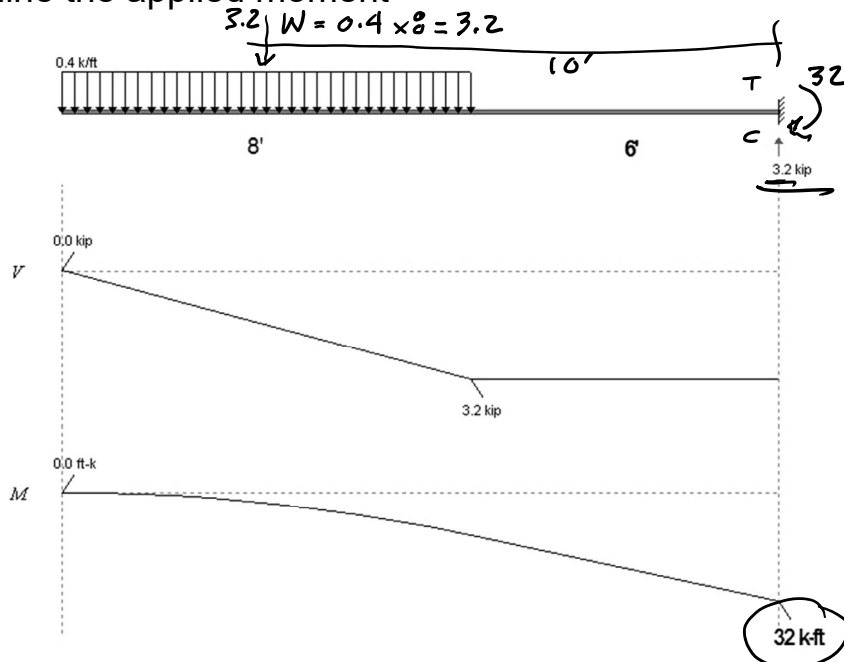
ALLOWABLE STRESS DESIGN SELECTION TABLE For shapes used as beams									
$F_y = 50$ ksi			$S_x$	Shape	Depth $d$	$F_y$	$F_y = 36$ ksi		
$L_c$	$L_u$	$M_R$					$L_c$	$L_u$	$M_R$
Ft	Ft	Kip-ft	In <sup>3</sup>		In	Ksi	Ft	Ft	Kip-ft
2.9	3.6	47	17.1	W 12×16	12	—	4.1	4.3	34
5.4	14.4	46	16.7	W 6×25	6 <sup>3</sup> / <sub>8</sub>	—	6.4	20.0	33
3.6	4.4	45	16.2	W 10×17	10 <sup>1</sup> / <sub>8</sub>	—	4.2	6.1	32
4.7	7.1	42	15.2	W 8×18	8 <sup>1</sup> / <sub>8</sub>	—	5.5	9.9	30
2.5	3.6	41	14.9	W 12×14	11 <sup>7</sup> / <sub>8</sub>	54.3	3.5	4.2	30
3.6	3.7	38	13.8	W 10×15	10	—	4.2	5.0	27
5.4	11.8	37	13.4	W 6×20	6 <sup>1</sup> / <sub>4</sub>	62.1	6.4	16.4	27
5.3	12.5	36	13.0	M 6×20	6	—	6.3	17.4	26
1.9	2.6	33	12.0	M 12×11.8	12	—	2.7	3.0	24
3.6	5.2	32	11.8	W 8×15	8 <sup>1</sup> / <sub>8</sub>	—	4.2	7.2	23
2.8	3.6	30	10.9	W 10×12	9 <sup>7</sup> / <sub>8</sub>	47.5	3.9	4.3	22

## Beam Design – steel example

Using **Steel W section**:

1. Choose a steel grade: Using  $F_y = 50$  ksi  $F_b = 0.6 F_y$

2. Determine the applied moment



## Beam Design – steel example

Using Steel W section:

2. Calculate section modulus,  $S_x$

$$S_x = \frac{M}{F_b}$$

$$S_x = \frac{M}{F_b} = \frac{32 \text{ k} \cdot (12)'}{0.6 (50 \text{ ksi})}$$

$$S_x = 12.8 \text{ in}^3$$

## Beam Design – steel example

Using Steel W section:

3. Choose a safe section. (from  $S_x$  table)

$$S_x \geq 12.8 \text{ in}^3$$

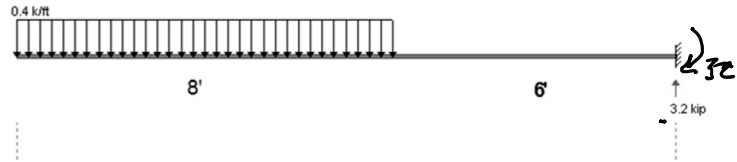
ALLOWABLE STRESS DESIGN SELECTION TABLE For shapes used as beams									
$F_y = 50 \text{ ksi}$			$S_x$	Shape	Depth $d$	$F_y$	$F_y = 36 \text{ ksi}$		
$L_c$	$L_u$	$M_R$					$L_c$	$L_u$	$M_R$
Ft	Ft	Kip-ft	in <sup>3</sup>		in	Ksi	Ft	Ft	Kip-ft
2.9	3.6	47	17.1	W 12×16	12	—	4.1	4.3	34
5.4	14.4	46	16.7	W 6×25	6¾	—	6.4	20.0	33
3.6	4.4	45	16.2	W 10×17	10½	—	4.2	6.1	32
4.7	7.1	42	15.2	W 8×18	8½	—	5.5	9.9	30
2.5	3.6	41	14.9	W 12×14	11¾	54.3	3.5	4.2	30
3.6	3.7	38	13.8	W 10×15	10	—	4.2	5.0	27
5.4	11.8	37	13.4	W 6×20	6¼	62.1	6.4	16.4	27
5.3	12.5	36	13.0	M 6×20	6	—	6.3	17.4	26
1.9	2.6	33	12.8	M 12×11.8	12	—	2.7	3.0	24
3.6	5.2	32	11.8	W 8×15	8½	—	4.2	7.2	23
2.8	3.6	30	10.9	W 10×12	9¾	47.5	3.9	4.3	22



# Beam Design – Glulam

Using **Glulam Timber**:

$F_b = 1250$  psi ( DF grade L3 )



$$S_x = \frac{M}{F_b}$$

$$S_x = \frac{M_{APPLIED}}{F_b} = \frac{32000 \text{ (lb)} \cdot (12)''}{1250 \text{ psi}} = 307.2 \text{ in}^3$$

**Table 5B Reference Design Values for Structural Glued Laminated Softwood Timber**

(Members stressed primarily in axial tension or compression) (Tabulated design values are for normal load duration and dry service conditions. See NDS 5.3 for a comprehensive description of design value adjustment factors.)

Use with Table 5B Adjustment Factors

Combination Symbol	Species	Grade	All Loading			Axially Loaded			Bending about Y-Y Axis				Bending About X-X Axis		Fasteners									
			Modulus of Elasticity		Compression Perpendicular to Grain	Tension Parallel to Grain	Compression Parallel to Grain		Loaded Parallel to Wide Faces of Laminations			Loaded Perpendicular to Wide Faces of Laminations												
			For Deflection Calculations	For Stability Calculations					Bending		Shear Parallel to Grain <sup>(1)(2)(3)</sup>	Bending	Shear Parallel to Grain <sup>(3)</sup>											
									E (10 <sup>6</sup> psi)	E <sub>min</sub> (10 <sup>6</sup> psi)				F <sub>E</sub> (psi)		2 or More Laminations F <sub>t</sub> (psi)	4 or More Laminations F <sub>c</sub> (psi)	2 or 3 Laminations F <sub>c</sub> (psi)	4 or More Laminations F <sub>by</sub> (psi)	3 Laminations F <sub>by</sub> (psi)	2 Laminations F <sub>by</sub> (psi)	F <sub>vy</sub> (psi)	2 Laminations to 15 in. Deep <sup>(4)</sup> F <sub>bx</sub> (psi)	F <sub>vx</sub> (psi)
Visually Graded Western Species																								
1	DF	L3	1.5	0.79	560	950	1550	1250	1450	1250	1000	230	1250	265	0.50									
2	DF	L2	1.6	0.85	560	1250	1950	1600	1800	1600	1300	230	1600	265	0.50									
3	DF	L2D	1.9	1.00	650	1450	2300	1900	2100	1850	1550	230	2000	265	0.50									
4	DF	L1CL	1.9	1.00	590	1400	2100	1950	2200	2000	1650	230	2100	265	0.50									
5	DF	L1	2.0	1.06	650	1650	2400	2100	2400	2100	1800	230	2200	265	0.50									

## Section Properties

Using Glulam Timber:

Glulam Timbers – 8 3/4" wide

$S_x$  required = 307.2 in<sup>3</sup>

8 3/4" x 15"

**Table 1C Section Properties of Western Species Structural Glued Laminated Timber (Cont.)**

Depth	Area	X-X Axis			Y-Y Axis	
d (in.)	A (in. <sup>2</sup> )	I <sub>x</sub> (in. <sup>4</sup> )	S <sub>x</sub> (in. <sup>3</sup> )	r <sub>x</sub> (in.)	I <sub>y</sub> (in. <sup>4</sup> )	S <sub>y</sub> (in. <sup>3</sup> )
8-3/4 in. Width					(r <sub>y</sub> = 2.526 in.)	
9	78.75	531.6	118.1	2.598	502.4	114.8
10-1/2	91.88	844.1	160.8	3.031	586.2	134.0
12	105.0	1260	210.0	3.464	669.9	153.1
13-1/2	118.1	1794	265.8	3.897	753.7	172.3
15	131.3	2461	328.1	4.330	837.4	191.4
16-1/2	144.4	3276	397.0	4.763	921.1	210.5
18	157.5	4253	472.5	5.196	1005	229.7
19-1/2	170.6	5407	554.5	5.629	1089	248.8
21	183.8	6753	643.1	6.062	1172	268.0

# Section Properties

## PROPERTIES OF SAWN LUMBER SECTIONS



### Sawn Lumber

Nominal Size b × d	Actual Size b × d	Area in. <sup>2</sup>	$I_x$ in. <sup>4</sup>	$S_x$ in. <sup>3</sup>
1 × 4	3/4 × 3 1/2	2.63	2.68	1.53
1 × 6	" × 5 1/2	4.13	10.40	3.78
1 × 8	" × 7 1/4	5.44	23.82	6.57
1 × 10	" × 9 1/4	6.94	49.47	10.70
1 × 12	" × 11 1/4	8.44	88.99	15.83
2 × 4	1 1/2 × 3 1/2	5.25	5.36	3.06
2 × 6	" × 5 1/2	8.25	20.80	7.56
2 × 8	" × 7 1/4	10.88	47.64	13.14
2 × 10	" × 9 1/4	13.88	98.93	21.39
2 × 12	" × 11 1/4	16.88	177.98	31.64
3 × 4	2 1/2 × 3 1/2	8.75	8.93	5.10
3 × 6	" × 5 1/2	13.75	34.66	12.60
3 × 8	" × 7 1/4	18.13	79.39	21.90
3 × 10	" × 9 1/4	23.13	164.89	35.65
3 × 12	" × 11 1/4	28.13	296.63	52.73
4 × 4	3 1/2 × 3 1/2	12.25	12.50	7.15
4 × 6	" × 5 1/2	19.25	48.53	17.65
4 × 8	" × 7 1/4	25.38	111.15	30.66
4 × 10	" × 9 1/4	32.38	230.84	49.91
4 × 12	" × 11 1/4	39.38	415.28	73.83

## Modes of Failure

### Strength

- Tension rupture
- Compression crushing

### Stability ✓

- Column buckling
- Beam lateral torsional buckling  
— LTB

### Serviceability

- Beam deflection
- Building story drift
- cracking

