Architecture 314 Structures I



Flexural Stress

- Loads pass through the **centroid** of the section
- Member is straight
- Member deflects in the plane of loading (vertical) – no lateral tensional buckling (LTB) —

$$f_b = \frac{Mc}{I}$$

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Axial + Flexure



The deflection caused by flexure together with the axial compression results in a secondary moment

$$M_2 = P \Delta$$

AXIAL FLEXURE $f = \frac{P}{A} \pm \frac{Mc_x}{I_x} \pm \frac{P\Delta c_x}{I_x}$



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Eccentric Loads

- Load offset from centroid
- M_e = P e
- Total load = P + M_e

combined stress (interaction) formula:



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Combined Stress

- Stresses combine by superposition
- · Values add or subtract by sign







dashed lines follow maximum compression; solid lines maximum tension

Principal Stresses

The surfaces of maximum tension and maximum compression stresses are at right angles, 90°.



- C.

Given the normal and shear stresses on the faces of any elemental square, the principal normal stresses can be calculated by:

$$s'_{N_{\text{max}}} = \frac{s_x + s_y}{2} \pm \sqrt{\left(\frac{s_x - s_y}{2}\right)^2 + s_s^2}$$

$$\dot{s_{N_{\min}}} = \frac{s_x + s_y}{2} \sin\left(\frac{s_x - s_y}{2}\right)^2 + s_s^2$$





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NA

f₄ ← f 🔲 b

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Mohr's Circle – Graphic Method to find Principal Stress

- 1. Choose two adjacent sides of the elemental square (H_& V)
- 2. Plot the coordinates (s_y, s_s) and (s_x, s_s) with S_N as abscissa and S_s as ordinate. Take normal tension stress and clockwise shear stress as positive.
- 3. Connect the two points with a line and find the center, C
- 4. Draw a circle with center at C, passing through H and V
- 5. Calculate tan $2\theta = FV/CF$
- 6. Read principal stress values at A and B and max shear stress at D



Principal Stresses



Pier Luigi Nervi, Gatti Wool Factory, Rome



Lines of principle stress

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Principal Stresses



Pier Luigi Nervi, Palace of Labor Floor System Palace of Labor (Palazzo del Lavoro)

The Ribbed Floor Slab Systems of Pier Luigi Nervi; Allison B. Halpern, David P. Billington, Sigrid Adriaenssens in "Beyond the Limits of Man" IASS Symposium 2013